

## CHEM 450 Handout SIGNIFICANT FIGURES

The term *significant figures* in a measurement refers to the number of digits needed to express the measured value in scientific notation.

*Example:* The scientific form of 0.000578 is  $5.78 \times 10^{-4}$ . There are 3 significant figures corresponding to the three digits 5, 7 & 8 in the scientific notation)

### Rules in determining the number of significant figures:

1. **Exact numbers** (Ex. 12 or a dozen) have *infinite number of significant figures* and therefore do not influence the number of significant figures in your measurement or calculation.
2. Since **nonzero digits are always significant**, we only have to worry about zeros.
3. The following summarizes the rules on significant figures, in terms of **zeros**:

a. **Leading zeros** - zeros before the first nonzero digit are not significant

*Example:* 0.00034 has 2 SF ( $= 3.4 \times 10^{-4}$ ); 0.0105 has 3 SF ( $= 1.05 \times 10^{-2}$ )

b. **Trailing zeros** = final zeros

(i) In whole numbers - zeros are not significant unless specified as significant by placing a bar or a decimal point

*Example:* There are 3 SF in  $56\bar{0}$ . ( $= 5.60 \times 10^2$ ); 2 in 1200 ( $= 1.2 \times 10^3$ ); 2 in  $1\bar{0}$   
( $= 1.0 \times 10^1$ ); 3 in 300. (*Notice the decimal point in the end*  $= 3.00 \times 10^3$ )

(ii) Decimals - zeros to the right of a decimal point are always significant, except for leading zeros discussed in 1.

*Example:* 12.00 has 4 SF; 0.00500 has 3 SF; 0.000709100 has 6 SF;  $1.060 \times 10^{-5}$  has 4 SF

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## Mathematical Operations Involving Significant Figures

### 1. Addition and subtraction

The final answer should have the same number of decimal places as the least precise measurement (i.e. the measurement with the least no. of decimal places)

*Example:*

12	No decimal place	56.75	2 decimal places
$+ \underline{2.4}$	One decimal place	$- \underline{1.2}$	1 decimal place
14	(No decimal place)	55.6	(55.55 rounded off to 1 decimal place)

### 2. Multiplication and division

The final answer must have the *same number of SF as the measurement with the least number of SF*, i.e. the least precise measurement

*Example:*  $6.7 \times 2.56 \times 3.333 = 57.167616$  or **57** (Final answer can only have 2 SF)

↗  
This term only has **2 SF** (the least SF)

$$(16.75 \times 1.4 \times 10^{-4}) \div 2.15 = 1.09069... \times 10^{-3} \text{ or } \mathbf{1.1 \times 10^{-3}}$$

↗ ↖ ↖

4 SF      2 SF (least)      3 SF

} (Final answer must have **2 SF**)

### 3. Logarithms and antilogarithms

Given the logarithm of n equal to a:

$$\log n = a \quad \text{or} \quad n = 10^a$$

The number n is the *antilogarithm* of a. There are two components of a logarithm: a **characteristic** and **mantissa**. The characteristic is the integer part while the mantissa is the decimal part. In the example below, these two components are indicated by arrows.

$$\log 25 = \mathbf{1.3979}$$

↗      ↖

**Characteristic = 1**      **Mantissa = 0.3979**

The *number of digits in the mantissa should equal the number of significant figures in the logarithm*. Thus, in the example above, since the logarithm (25) has 2 significant figures, the mantissa should be rounded off to 2 digits. Therefore, the equation should be written as:

$$\log \mathbf{25} = \mathbf{1.40}$$

↗      ↖

This *logarithm* has 2 SF      The *mantissa* (right of decimal point) must have 2 *digits*